The Impact of the Mode 4 Liberalization of Services on Economic Growth, and Policy Options

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Abstract

This paper develops a model based on realistic assumptions of international movement of natural persons such as the heterogeneity of and private information on agent types, and outlines the scope for national policy and the role of private agents. The paper argues that it is always beneficial for a country to have a liberal policy on the acceptance of natural persons, and admit high quality human capital. However, due to private information on the quality of human capital, professional organizations and private agents may maintain certain standards of observable attributes of would-be migrants. Those standards are costly to adhere to, thus serve as a screening device for choosing high quality human capital.

The model demonstrates that high quality human capital in a poor country tends to migrate under Mode 4 liberalization to rich countries. However, if the poor country is above a threshold poverty level, actual migration may or may not take place, i.e. there could be multiple equilibria. The source of multiple equilibria is the strategic complementarity and failure in coordinating actions of a large number of agents. Therefore, a poor country, while having a liberal policy on movement of natural persons, could strengthen economic and social infrastructure to avoid herd behavior and mass migration of high quality human capital.

Liberal policies on movement of natural persons could reduce welfare of a host country if not accompanied by costly screening mechanisms. With such costly screening, movement of natural persons always increases welfare of the all agents in host countries, as well as welfare of migrants, but reduces the welfare of agents with low quality human capital in source countries. (JEL F 22, 015, 040)

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I. Introduction

Services play a dominant role in economic growth and development of a country. Quah (1997) shows that most of the economic growth in many developed and developing countries arises from growth in the services sector. In view of the benefits of larger markets, the World Trade Organization (WTO) encourages countries to grant foreign service suppliers greater access to their markets. The fundamental economic reasoning is similar to the reasons discussed in Smith (1776), and reasons behind the benefits of trade in goods. However, services can be supplied by more ways, or modes, than goods, which are supplied only through cross-border mode (Mode 1). The other modes of supplying services are through consumption abroad (Mode 2), commercial presence (Mode 3) and movement of natural persons (Mode 4). To allow services flow through all four modes, countries have to undertake complicated liberalization measures in several markets such as financial market, labor market, and in immigration procedures.

Services sector spans across a wide spectrum (WTO Secretariat 1991). WTO Secretariat (1991) has listed twelve categories of services. Production of many of those services requires high quality human capital. Thus, Mode 4 liberalization would amount to significant extent of high quality human capital moving across countries. The duration of stay by a service provider in a foreign country is temporary as explained by the WTO Secretariat (2002). However, WTO Secretariat (2002, pp 2) further explains that ‘there is no specified time frame in the GATS of what constitutes ‘temporary’ movement; this is defined negatively, through the explicit exclusion of permanent presence’. Thus, the duration of stay of a service provider could be a longer period, as long as the stay is not extended to arouse political economy issues of migration as discussed in Winters (2002). Thus, I use the term ‘migration’ in this paper to indicate movement of natural persons for considerably longer periods of time. This consideration is realistic since natural persons providing services tends to stay longer periods in host countries once they establish service centers, or join service centers domiciled in host countries. Any short-term movement is more akin to Mode 1 supply of goods, and does not enable an interesting analysis on the impact of Mode 4 liberalization.

As WTO Secretariat (2002) indicates, Mode 4 is the least liberalized mode, which indicates that there is a reluctance to admit natural persons liberally. However, there exists a general bias in favor of admitting high quality human capital such as executives, managers and specialists. This is achieved by establishing screening devices to separate high quality human capital from low quality human capital.

The objectives of this paper are to construct a model of migration of high quality human capital, to use the model to evaluate the welfare and growth implications of migration in economies, and to focus on appropriate economic policies for countries. I explain the motivation to migrate to supply services and motivation to invite such migrants using the model. The model portrays stylized facts of migration such as a host country’s reluctance to grant free entry, but preference for screening of natural persons to choose high quality human capital. The model enables us to examine long run dynamic impact of migration, which is different from other models such as Winters (2002) which takes into account only the static impact.
The principal factor driving economic growth in the model is the accumulation of human capital. Accumulation of human capital is a principal source of economic growth according to a class of growth models made popular by Lucas (1988). Theories of migration have not established a link between migration and economic growth. However, we notice that economists have already indicated that migration of high quality human capital causes an adverse impact on source countries and a positive impact on host countries. During the seventies, Bhagwati (1976) and Bhagwati and Partington (1976) highlighted the possibility of an adverse economic impact of the migration on poor countries. They went to the extent of suggesting a compensation scheme for poor countries as the loss of human capital causes a loss of welfare. Borjas (1994) suggested that “immigrants with a high level of productivity and who adapt rapidly to conditions in the host countries’ labor market can make a significant contribution to the economic growth”.

The model presented in the paper assumes heterogeneity of and private information on agent types in countries. Agents evaluate the costs and benefits of migration before making a decision on whether to leave the ‘source’ country or to accept a migrant in the ‘host’ country. Although there could be various types of costs, the cost of migration considered in this paper arises due to existence of private information on agent types. Different agents in a country are initially endowed with different levels of unobservable human capital and the same level of observable human capital. Agents are of different types based on the endowment of the level of unobservable human capital. The agent type is known only to the agent. Hence, if an agent wishes to migrate, she should issue a costly signal indicating her type as in the Spence (1973, 1974) models of “job market signaling”. The signal is the level of observable human capital, which has an opportunity cost of acquiring.

As in Lucas’s (1988) and Tamura’s (1991, 1994) models of endogenous growth, each country has a positive production externality in human capital accumulation associated with its average level of human capital. Therefore, a country with a higher average level of human capital gives greater benefits to its inhabitants. All agents in any country prefer either to increase the average level of human capital in their own country, or to migrate to a country with a higher average level of human capital, depending on which will increase their welfare. By definition a ‘poor’ country has a lower level of average human capital than a ‘rich’ country. Hence it follows that, when the cost of migration is lower than benefits, all agents with higher levels of human capital in the poor country will tend to migrate to rich countries. Rich countries will only allow the migration of agents with high levels of human capital.

The existence of a positive production externality generates a “strategic complementarity” in human capital. Strategic complementarity is the phenomenon where any one agent’s actions affect other agents’ actions. The impact of this on equilibria is as follows. If some agents with high quality human capital migrate to a richer country from a poor country, it will

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1/ A model of international migration was presented in Braun (1993). He imposes a limitation of migration through a congestion of a natural resource. This congestion eliminates long run growth.
2/ Similar externalities were used in intra-country urban-rural migration models of Todaro (1969) and Glomm (1992). Harris and Todaro (1970) use a politically motivated minimum wage in the urban sector.
decrease the average level of human capital in the poor country. This further encourages other agents with high quality human capital to migrate. Similarly, if agents with higher levels of human capital do not migrate, it will diminish any other agent’s desire to migrate.

An interesting result arising from the strategic complementarity is the existence of multiple equilibria in poor countries, when agents’ actions are not coordinated, or when there is a coordination failure. For example, if a country is not so poor, costs of migration will outweigh the benefits of migration if all agents with high quality human capital decide not to migrate. This will lead to a no-migration equilibrium. However, if all but one agent decides to migrate, the benefits will outweigh the costs for the particular agent due to the strategic complementarity, leading to a symmetric Nash equilibrium where all agents migrate.

The model further reveals that if a country is poorer than a “threshold poverty level”, the strategic complementarity and coordination failure may not be strong enough to generate a no-migration equilibrium. At those poverty levels, the benefits of migration will outweigh the costs irrespective of whether other agents with high quality human capital migrate or not. Hence, the only resulting equilibrium is a migration equilibrium.

The model has following growth features. In a closed economy high type agents’ income grows at a lower rate while low type agents’ income grows at a higher rate until both agent types converge to a common long run growth rate. The rich country will have a higher growth rate than the poor country during the transition. In a perfect information environment, high quality agents tend to migrate to a richer country. Migration greatly reduces both per capita income and low type agents’ income in the poor country. It increases migrants’ income and growth rate. However, after migration the growth rate of per capita income in a poor country is higher than the growth rate without migration. This is due to the slower growth of agents with higher levels of human capital in a closed economy which in turn slows down per capita income growth. Once migration takes place, there is only one type of agents in the poor country, and their human capital grows at the long run growth rate. Migration increases the per capita income and income of all agents in the rich country.

A comparison of welfare in different equilibria reveals that the rich country always gains from migration. Agents with lower levels of human capital in the poor country always lose welfare in a migration equilibrium. However, the effect on the welfare of agents with a high level of human capital in the poor country depends on the relative poverty of their country. If a poor country’s proportion of low-type agents is less than a critical value (i.e. if the poor country is not so poor), the welfare of agents with higher levels of human capital in a migration equilibrium is lower than the welfare in the no-migration equilibrium. But, if the proportion is larger than the critical value, those agents’ welfare is greater in a migration equilibrium than in a no-migration equilibrium.

The model further reveals that policy option of complete liberalization could possibly reduce the welfare of the rich or host country, due to the possible migration of low level human capital. Thus, the host country, or professional groups in the host country could set up costly screening systems to choose only the high level human capital. The policy of the poor country could be a political outcome as there are different types of agents who also

4/ The critical value is a proportion of agents above the threshold poverty level determined by model parameters.
differ in terms of welfare gains as a result of any economic policy. To avoid mass migration due to strategic complementarity, a poor or source country could improve economic and social environment to provide additional incentives for the high quality human capital to remain in their country.

The rest of the paper is structured as follows. Part 2 describes the model environment. The costs and benefits of migration and agent behavior are discussed in part 3. In part 4, migration under the assumption of full information on agent types is considered. Migration under private information and under the two policy alternatives of complete liberalization and liberalization with costly screening are considered in part 5. Part 6 investigates the strategic complementarity and its role on generating multiple equilibria and threshold poverty level. In part 7, welfare, growth and policy options are discussed. Part 8 concludes the study.

II. Environment of the Migration Model

The model is adopted from Thenuwara (1997). The model considers two countries with a population of agents in each country normalized to 1. Time is discrete and indexed by \( t=0,1,2,\ldots \). In both countries, agents are of two types and are indexed by \( i (i=1,2) \). The lower type \( (i=1) \) has a lower initial level of human capital and the higher type \( (i=2) \) has a higher initial level of human capital. The fraction of type 1 agents (agents with lower level of human capital) in the two countries are denoted as \( q_{1} \) and \( q_{1}^{*} \) respectively, and \( q_{1} > q_{1}^{*} \). The two countries are labeled ‘rich’ and ‘poor’ based on the average level of human capital prevailing in a country at the beginning of time 0.

At the beginning of time 0, agent type \( i \) in any country is endowed with \( s_{i0} \) level of observable human capital and \( h_{i0}^{u} \) level of unobservable human capital. The total human capital of an agent is \( h_{i0} = s_{i0} + h_{i0}^{u} \). Both agent types have the same level of observable human capital, but different levels of unobservable human capital. The level of unobservable human capital is considered private information. All agents are also endowed with one unit of labor hours in each period of time.

In the period 0, agents invest their time in upgrading human capital. They begin producing and consuming goods starting from period 1. In the period 0, they privately produce human capital and may decide on migrating and acquire observable human capital to use as a signal.

Production technologies in period 0 are as follows.

\[
\begin{align*}
    h_{i1}^{u} &= a \cdot x_{i} h_{i0} \\
    s_{i} &= b \cdot (1 - x_{i}) h_{i0}
\end{align*}
\]

where \( a > b > 1 \), \( h_{i0} = s_{i0} + h_{i0}^{u} \), and fraction of labor hours invested in the unobservable human capital by an agent type \( i \) is \( x_{i} \).

At the beginning of period 1, if they have already decided, they issue signals and migrate. Starting from period 1, they enter into the production of consumption goods and human capital. They will then be subject to the production externality. Agent type \( i \) devotes
fraction of labor hours to the production of the consumption good, and production takes the following form.

\[ y_{it} = u_i h_{it}, \]  \hspace{1cm} \text{where} \ h_{it} = h_{it}^u + s_{it}. \quad (2.3) \]

The production of observable and unobservable human capital after period 0 is given by (2.4a) and (2.4b).

\[ h_{it+1}^u = a_i (x_{it} (1 - u_{it}) h_{it})^\alpha H_{t}^{1-\alpha} \quad (2.4a) \]
\[ s_{it+1} = b_i ((1 - x_{it}) (1 - u_{it}) h_{it})^\alpha H_{t}^{1-\alpha} \quad (2.4b) \]

where \( 0 < \alpha < 1 \) and \( H_t \) is the average level of human capital in a country, which is an externality as in Lucas (1988).

The two equations (2.4a) and (2.4b) could be combined to obtain the aggregate human capital accumulation given in (2.5).

\[ h_{it+1} = A_i ((1 - u_{it}) h_{it})^\alpha H_{t}^{1-\alpha} \quad (2.5) \]

where \( A = (a_i^{1/1-\alpha} + b_i^{1/1-\alpha})^{1-\alpha} > 1. \)

Agents derive utility from consuming goods over the life time starting from period 1. The utility is given by the following.

\[ U = \sum_{t=1}^{\infty} \beta^{t-1} \ln c_{it}, \]  \hspace{1cm} \text{where} \ 0 < \beta < 1 \ \text{is the rate of time preference and} \ c_{it} \ \text{is the consumption by the agent} \ i \ \text{at time} \ t. \]

III. The Migration Model

A. Cost of Migration

The cost of migration arises from having asymmetric information on agent types. An agent is able to migrate if he can convince the rich country that he is the high type. This is done by issuing a signal. The signal is the level of observable human capital. At the beginning of time 0, all agents look alike as they are endowed with the same amount of observable human capital. Hence, if the high type wishes to issue a signal they have to acquire more observable human capital during the period 0. There is an opportunity cost of acquiring observable human capital. In order to obtain a formula for the cost of signaling in terms of foregone human capital, consider an agent \( i \) investing time \( x_i \) in producing the observable human capital. The signal \( s_i \) defined as the observable human capital is given in (2.2).

5/ In real life agents in poor countries spend time on preparing for various screening tests, acquiring knowledge in foreign languages, and acquiring other educational qualifications which do not directly enhance their level of human capital.
The signal \( s_i \) lies in the interval \([0, \bar{s}_i]\), where the upper bound of the signal is given by \( \bar{s}_i = bh_{i0} \). The cost of signaling defined as \( f(s_i) \) arises due to the lower efficiency in producing observable human capital.

\[
f(s_i) = h_{i1,\text{max}} - \left\{ a(x_i h_i) + b(1 - x_i)h_{i0} \right\}
\]

(3.1)

\[
f(s_i) = s_i \frac{(a - b)}{b}
\]

(3.2)

where \( h_{i1,\text{max}} = ah_{i0} \)

Since \( a > b \), it follows that \( f(0) = 0 \), \( f' > 0 \), and \( f'' = 0 \)

After issuing a signal of strength \( s_i \), the human capital an agent could acquire is given by (3.3).

\[
h_{it} = h_{i1,\text{max}} - f(s_i)
\]

(3.3)

**B. Benefits of Migration**

Benefits of migration arise from being able to live in an environment with a higher level of human capital externality. Both agent types in the poor country prefer to migrate to the rich country where the level of average human capital is higher. All agents in the rich country prefer to have only the high type agents from the poor country migrate to the rich country. We assume that migration takes place at the beginning of the time period 1.\(^6\) In order to compute the benefits of migration, we consider indirect utility of an agent living in a country with average human capital \( \{H_t\}_{t=1}^\infty \). The indirect utility is given by the solution to the problem (CP) defined below.

\[
V_i(h_{it}) = \text{Max}_{c_{it}, h_{it+1}} \left[ \ln c_{it} + \beta V_i(h_{it+1}) \right]
\]

subject to

(CP)

\[
c_{it} = u_{it} h_{it}
\]

\[
h_{it+1} = A(1 - u_{it})^\alpha h_{it} \circ H_t^{1-\alpha}
\]

\[
h_{il} = h_{i1,\text{max}} - f(s_i) \text{ is given.}
\]

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\(^6\) Even if we drop this assumption it can be shown that the best time to migrate is the beginning of time period 1, for the difference between average levels of human capital in the two countries increases over time.
where $H_i$ is the average level of human capital in agent $i$'s country of residence. The agent solves CP by taking the average level of human capital as given. The Lagrangian can be written as,

$$L = \max_{\{c_{it}, u_{it}, h_{it+1}\}} \left\{ \ln c_{it} + \beta V_i(h_{it+1}) + \lambda_{it} [h_{it} - c_{it}] + \mu_{it} A((1 - u_{it}) h_i)^{\alpha} H_i^{1 - \alpha} - h_{it+1} \right\}$$

Initial level of human capital after issuing a signal of strength $s_i$ is $h_{i1} = h_{i1,\text{max}} - f(s_i)$

First order conditions (f.o.cs) are as follows.

F.o.c for consumption,

$$f.o.c. \quad (3.4)$$

$$\lambda_{it} h_{it} - \mu_{it} \alpha A(1 - u_{it})^{\alpha - 1} h_{it}^{\alpha} H_i^{1 - \alpha} = 0 \quad (3.5)$$

F.o.c for labor choice,

$$f.o.c. \quad (3.6)$$

$$\beta V_i'(h_{it+1}) - \mu_{it} = 0$$

Transversality condition is given by

$$\lim_{t \to \infty} \lambda_{it} h_{it+1} \to 0 \quad (3.7)$$

In order to solve the system of equations, the following result from the Envelope theorem is used.

$$V_i'(h_{it+1}) = \lambda_{it+1} u_{it+1} + \mu_{it+1} A(1 - u_{it+1})^{\alpha} h_{it+1}^{\alpha - 1} H_i^{1 - \alpha} \quad (3.8)$$

The solution implied by the first order conditions is given in (3.9) - (3.11). Appendix A gives the solution procedure.

$$u_{it} = 1 - \alpha \beta, \quad t=1,2,... \quad (3.9)$$

$$h_{it+1} = A(\alpha \beta)^{\alpha} h_{it}^{\alpha} H_i^{1 - \alpha}, \quad t=1,2,... \quad (3.10)$$

$$c_{it} = (1 - \alpha \beta) h_{it}, \quad t=1,2,... \quad (3.11)$$

As shown in Appendix A, (3.7) and (3.8) can be solved to produce

$$h_{it} = A^t (\alpha \beta)^{\alpha} h_{i1}^{\alpha} \prod_{s=0}^{t-1} \sum_j \theta_j h_{j1}^{\alpha} \left[ 1 - \alpha \right] \quad t=1,2,... \quad (3.12)$$

$$c_{it} = (1 - \alpha \beta) A^t (\alpha \beta)^{\alpha} h_{i1}^{\alpha} \prod_{s=0}^{t-1} \sum_j \theta_j h_{j1}^{\alpha} \left[ 1 - \alpha \right] \quad t=1,2,... \quad (3.13)$$
The value function of the agent type \( i \) in poor country \( (V_i) \) is given in (3.14).

\[
V_i = \sum_{t=0}^{\infty} \beta^t \ln \left( (1 - \alpha \beta) \left( A(\alpha \beta)^\alpha \right)^t \prod_{s=0}^{t-1} \left( \sum \theta_j h_j^{\alpha^t} \right)^{1-\alpha} \right)
\]

which is simplified in Appendix A to produce

\[
V_i = \ln k + \frac{1}{(1 - \alpha \beta)} \ln \left( h_{i1,\max} - f(s_i) \right) + \frac{(1 - \alpha) \beta}{(1 - \beta)} \ln H_i. \tag{3.14}
\]

where

\[
\ln k = (1 - \alpha) + \frac{\ln(1 - \alpha \beta)}{(1 - \beta)} + \frac{\beta}{(1 - \beta)^2} \ln A(\alpha \beta)^\alpha
\]

It is noted that the value function depends positively on the initial level of human capital and the level of externality in the agent’s country of residence, and negatively on the cost of signaling.

**C. A Model of Agent Behavior**

The agent behavior under the assumption of private information is presented as a bayesian Nash game. It is assumed that different types of agents in the poor country will issue a signal simultaneously. All agents in the rich country will vote on accepting or rejecting the entry to the rich country by an agent in the poor country after observing signals. There is no conflict in voting patterns as all agents in the rich country wish to have only the high type agents migrated to their country.

A pure strategy of an agent in the poor country is issuing a signal from the space

\[
S_i = \left[ 0, s_i \right].
\]

A pure strategy of the rich country is accepting or rejecting an agent after observing the signal.

Agents in the rich country have the prior beliefs of agents given as \( P(i) = \theta_i \);

where \( P(i) \) is the probability that a randomly chosen agent is type \( i \).

The payoff function for an agent in a country \( (V_i) \) is the indirect utility given in (3.14).

**IV. Migration Equilibria under Complete Information**

It is clear from the value function derived in (3.14) that high type agents are always better off, the lower is the proportion of low type agents. However, it is assumed that although it enhances the utility of high type agents in a country, they cannot banish low type agents from the country because all agents equally share the ownership of the country.

If an agent wishes to migrate from the poor country, she has to show her economic usefulness to the rich country. When allowing for migrants to enter the country, both types in the rich country will agree on who to admit. By the construction of the model, all types in
the rich country will accept only those agents with a level of human capital higher than the average level of the rich country. In order to see this consider that \( j \) proportion of \( k \) (\( k \in \{1,2\} \)) type agents with \( h_{k0}^* \) level of human capital enters the rich country. An agent’s value function in the rich country as derived in (3.14) then has the following form.

\[
V^*_i = \ln k + \frac{1}{(1 - \alpha \beta)} \ln h_{i1}^* + \frac{(1 - \alpha) \beta}{(1 - \beta)} \ln \left( \sum_j \theta^*_j h_{j0}^* \right) \left( \frac{1 + \varphi}{1 + \varphi} + \frac{h_{k1}}{1 + \varphi} \right) 
\]

(4.1)

where \( h_{i1}^* \) is the level of human capital of agent type \( i \) in the rich country at the beginning of period 1. The derivative of the value function with respect to \( \varphi \) is

\[
\frac{dV^*_i}{d\varphi} = \frac{(1 - \alpha) \beta}{(1 - \beta)} \frac{1}{\sum_j \theta^*_j h_{i0}^*} \left( \frac{\varphi}{1 + \varphi} - \frac{h_{k0} - \sum_j \theta^*_j h_{i1}^*}{(1 + \varphi)^2} \right) 
\]

(4.2)

We know that \( \sum_j \theta^*_j h_{i1}^* \) is the rich country’s average level of human capital. Hence, it is clear from (4.2) that the value function of an agent type \( i \) in the rich country is decreasing at all value of \( \varphi \) when \( h_{k0} < \sum_j \theta^*_j h_{i0}^* \).

Hence in an equilibrium all high type agents in the poor country will migrate to the rich country. Welfare and growth implications of migration with full information are discussed in part 7.

V. Migration Equilibria under Incomplete Information and Coordination

A. Migration Equilibria under Incomplete Information and Full Liberalization

The agent types are considered private information in this part. In this environment the host country will liberally admit any agent from a source country. There are no costly screening requirements. Thus, the low type agents in a poor country will have a greater advantage in migrating to a richer country. This will increase welfare of migrants, and high type agents in the poor country, while reducing the welfare of all agents in the host country. Hence, it is natural that all countries will adopt a policy of costly screening when agent type is uncertain, and only private information.
B. Migration Equilibria under Incomplete Information, Coordination and Partial Liberalization with Costly Screening

It is clear that agents in the rich country are not willing to migrate to the poor country. Furthermore, as explained in the previous part, agents will be able to migrate only if they have at least the average human capital level of the rich country. It is also clear that the rich country will not admit agents from the poor country randomly (without any screening) as the expected human capital possessed by an agent is less than the average human capital in the rich country.

In this part we restrict our attention to the equilibria when all high type agents in the poor country could coordinate their actions. As explained in the next part, there could be multiple equilibria when the coordination fails.

In the following discussion, we show that under the rational beliefs of the rich country on the agent types of the poor country, two types of pure strategy equilibria could exist. In one equilibrium, all high type agents of the poor country will migrate to the rich country. This equilibrium is called the ‘migration equilibrium’. The other type of equilibrium is called the ‘no-migration equilibrium’ where no agent from the poor country will migrate. The existence of any type of equilibrium depends on the relative level of poverty of the poor country indicated by the proportion of low type agents ($q_1$).

Defining Equilibria

When defining equilibria we take into account the rational beliefs of the rich country, costs and benefits of adapting a particular strategy by an agent in the poor country, the rationality of such a strategy given beliefs of the rich country, the strategy of the rich country and the rationality of the strategy of the rich country.

When an agent issues a signal, he incurs a cost in terms of human capital accumulation within the period $\theta$ and as a result utility is reduced. Hence, his action is rationalized only if he could receive a compensating benefit. The benefit of the action is that the agent could be transferred to an environment with a greater externality. For example, if a high type agent in the poor country issues a signal, he will do so if he could migrate to the rich country where the human capital externality is greater. A low type agent will signal either if he could migrate or if he could deter high type agents from migrating. In both cases he will enjoy a higher level of human capital externality.

An equilibrium is defined by adapting the signaling equilibrium defined in Osborn and Rubinstein (1995).

Definition

A Perfect Bayesian Signaling Equilibrium is the set of strategies by the agents in the poor country, set of posterior beliefs by agents in the rich country on agent types of the poor country after observing the signals, strategy of agents in the rich country, and resulting externalities in the two countries $\{H_t, H_t^*\}_{t=1}^{\infty}$ such that the following conditions are satisfied.
R1. Sequential Rationality. - given rich country’s beliefs, the strategy set of agents in both countries is at least as good as any other action. This implies that
   a. each agent in the poor country maximizes his utility given his strategy, strategies of other agent types in the poor country and beliefs and strategies of the agents in the rich country;
   b. Agents in the rich country maximizes their utility given their beliefs and strategies, and strategies of the agents in the poor country.

R2. Consistency - \( \left\{ H_t, H_t^* \right\}_{t=1}^{\infty} \) are consistent with agents’ strategies, and beliefs.

R3. Bayesian Updating - after observing and considering the rationality of action taken by agents in the poor country, agents in the rich country updates their beliefs on the type of the agent who took the action, according to Bayes Rule.

A migration equilibrium is a perfect bayesian equilibrium where two types of agents in the poor country choose to issue different signals. The rich country could correctly identify the high type agents, who will be able to migrate. In a no-migration equilibrium both types issue the same signal and the rich country will not allow migration of any agent. This is because the expected level of human capital of a migrant with prior probabilities is less than the average level of human capital in the rich country.

C. Rational Beliefs of the Rich Country and Screening

We argue in this section that the rich country could impose a minimum signal required for migration that separates the low type from the high type. At this minimum signal, the low type will always find it too costly to migrate. The high type may or may not migrate depending on the benefits of migration. For example, if a country is relatively poor, the benefits of migration are larger, thus providing an incentive for signaling and migrating. However, if the gap between the two countries is not too large, the benefits of migration may not outweigh the costs, thus providing no incentive for migration.

Potential benefits of issuing a signal by the low type are twofold. One benefit is that they may be able to migrate. The other benefit is that they could deter migration of the high type by issuing the same signal as the high type. The minimum signal imposed by the rich country should be large enough that the low type will not be able to migrate. The rich country’s beliefs are rational if they assume that only high type will issue a signal larger than the minimum signal. As a first step of characterizing the minimum signal \( (s_{min}) \) we consider the signal that will deter any low type agent migrating to the rich country.

Suppose that a low type agent issue a signal \( s_t \) and migrate to the rich country. The cost of the signal is \( f(s_t) \) and the benefit arises from being able to enjoy the relatively higher externality in the rich country.

Their utility after migration, \( V_f(s_t, H_t^*) \), is given in (5.1).

\[
V_1(s_t, H_t^*) = \ln k + \frac{1}{(1 - \alpha \beta)} \ln \left( h_{11, \text{max}} - f(s_t) \right) + \frac{(1 - \alpha)\beta}{(1 - \beta)} \ln H_t^*. \quad (5.1)
\]
In order for the agent to stay in the poor country, the minimum signal must be made large enough so that the utility from not issuing a signal and not migrating \((V_1(0, H_1))\) given in (5.2) should be at least as large as the utility given in (5.1).

\[
V_1(0, H_1) = \ln k + \frac{1}{1 - \alpha \beta} \ln \left( h_{11, \text{max}} \right) \\
+ \left( \frac{1 - \alpha}{1 - \beta} \right) \ln \left( \theta_1 h_2 + (1 - \theta_1) \left( h_{10, \text{max}} \right) \right).
\]

(5.2)

and, \(V_1(0, H_1) \geq V_1(s_1, H_1^*)\)

(5.3)

Solution to (5.3) yields \(s_{\text{min}}\).

Next, we consider the maximum signal that a low type agent would be willing to issue in order to mimic the high type. The signal is characterized by comparing the benefits of deterring migration when all low type agents issue a signal to deter the high type and the benefits of not issuing any signal and allowing the high type to migrate.

Denoting the maximum signal low type agents are willing to issue as \(s_{\text{pmax}}\) (maximum pooling signal), we can show that at this signal, the low type is indifferent between issuing and not issuing a signal.

When they issue a signal and deter the high type from migrating the cost is \(f(s_{\text{pmax}})\) and the benefit is the higher externality given by

\[
H_1 = \left( \theta_1 \left( h_{11, \text{max}} - f(s_{\text{pmax}}) \right) + (1 - \theta_1) \left( h_{21, \text{max}} - f(s_{\text{pmax}}) \right) \right)
\]

Hence an agent’s utility of signaling is given by

\[
V_1(s_{\text{pmax}}, H_1) = \ln k + \frac{1}{1 - \alpha \beta} \ln \left( h_{11, \text{max}} - f(s_{\text{pmax}}) \right) \\
+ \left( \frac{1 - \alpha}{1 - \beta} \right) \ln \left( \theta_1 \left( h_{11, \text{max}} - f(s_{\text{pmax}}) \right) + (1 - \theta_1) \left( h_{21, \text{max}} - f(s_{\text{pmax}}) \right) \right).
\]

(5.4)

When he does not signal, all high types will signal and migrate. His utility is then given by

\[
V_1(0, H_1) = \ln k + \frac{1}{1 - \alpha \beta} \ln h_{11, \text{max}} + \left( \frac{1 - \alpha}{1 - \beta} \right) \ln h_{11, \text{max}}.
\]

(5.5)

The maximum signal a low type is willing to issue is now given by

\[
V_1(0, H_1) \geq V_1(s_{\text{pmax}}, H_1).
\]

(5.6)

Hence the signal used in screening is the maximum of \(s_{\text{min}}\) and the \(s_{\text{pmax}}\). We can show...
that when two initial levels of human capital of the two agent types are sufficiently different, \( s_{\text{min}} < s_{\text{pmax}} \), hence we will consider \( s_{\text{pmax}} \) as the screening signal.

### D. Characterizing Equilibria

In this section, conditions under which different equilibria exist are outlined. We can characterize two types of equilibria, one where all high types migrate (migration equilibrium) and another where no one migrates (no-migration equilibrium). The type of equilibrium depends on whether the cost of signaling for the high type outweighs the benefits.

#### Migration Equilibrium

In order to show the existence of a migration equilibrium, consider that all high type agents issue a signal \( s_s \) larger than \( s_{\text{pmax}} \). According to the ‘intuitive criterion’ discussed by Cho and Kreps (1988), the high type will issue a signal just above \( s_{\text{pmax}} \) in a separating equilibrium.

In order to ensure the sequential rationality of the strategy, requirements R1 - R3 given in definition 5.1 should hold.

R1 a. i. High type agents of the poor country should maximize their utility.

In order to show this result, consider the benefit of issuing the signal, that is to receive the human capital externality of the rich country.

\[
H_1^* = \frac{1 - \theta_1^*}{2 - \theta_1} h_{21,\text{max}} + \frac{1 - \theta_1}{2 - \theta_1} \left( h_{21,\text{max}} - f(s) \right) + \frac{\theta_1^*}{2 - \theta_1} h_{11,\text{max}}
\]

The payoff for issuing the signal (utility after issuing a signal and migrating) is

\[
V_2(s_s, H_1^*) = \ln k + \frac{1}{(1 - \alpha \beta)} \ln \left( h_{21,\text{max}} - f(s_s) \right)
\]

\[
+ \frac{(1 - \alpha) \beta}{(1 - \beta)} \ln \left( \frac{1 - \theta_1^*}{2 - \theta_1} h_{21,\text{max}} + \frac{\theta_1^*}{2 - \theta_1} h_{11,\text{max}} + \frac{1 - \theta_1}{2 - \theta_1} \left( h_{21,\text{max}} - f(s_s) \right) \right).
\]

(5.7)

Issuing any other signal \((s)\) will result in denying the migration. The utility associated with this strategy is

\[
V_2(s, H_1) = \ln k + \frac{1}{(1 - \alpha \beta)} \ln \left( h_{21,\text{max}} - f_2(s) \right)
\]

\[
+ \frac{(1 - \alpha) \beta}{(1 - \beta)} \ln \left( (1 - \theta_1) \left( h_{21,\text{max}} - f_2(s) \right) + \theta_1 h_{11,\text{max}} \right).
\]

(5.8)

Sequential rationality requires \( V_2(s_s, H_1^*) \geq V_2(s, H_1) \) \( \forall s \in [0, \bar{s}] \)

R1 a. ii. Low type agents in the poor country maximize their utility.
This requires that if a low type agent issues the signal $s_s$ he will derive a lesser utility than when not issuing any signal. This follows from the screening by the rich country.

R1 b. Accepting a migrant after observing $s_s$ maximizes utility of all agents in the rich country.

This happens when the high type has at least the average human capital of the rich country after issuing the signal.

Requirements 2 and 3 of the perfect bayesian equilibrium are already incorporated in the requirements 1 i and 1 ii which were verified above.

No-migration Equilibrium

We can show that in a no-migration equilibrium, the cost of issuing a signal by high type agents is greater than the potential benefits.

High type agents’ utility after issuing a signal $s_s$ and after migrating is given in (5.7). Since low type agents do not issue a signal, the utility of not issuing a signal is

$$V_2(0, H_1) = \ln k + \frac{1}{1 - \alpha \beta} \ln h_{21, \text{max}} + \frac{(1 - \alpha) \beta}{1 - \beta} \ln \left( \theta h_{11, \text{max}} + (1 - \theta) h_{21, \text{max}} \right).$$  

Hence $V_2(0, H_1) \geq V_2(s_s, H_1^*)$  

(5.10)

The rich country does not admit any agents as no one issues a signal.

E. Existence of Equilibria

We can also show that if the proportion of the low type in the poor country is below a certain critical value, we can support a no-migration equilibrium. If the proportion is above this value, a migration equilibrium could exist. The proof of the existence is carried out in several steps.

First we show that, at higher levels of $q_j$, a migration equilibrium exits and at lower levels of $q_j$, a zero-migration equilibrium exists. In order to show this, we consider the maximum signal a high type agent is willing to issue so that she could separate herself from the low type ($s_{s, \text{max}}$) and the maximum signal a low type agent is willing to issue in order to mimic the high type ($s_{p, \text{max}}$). If $s_{s, \text{max}}$ is lower than $s_{p, \text{max}}$, then a zero-migration equilibrium exists. On the other hand, if $s_{p, \text{max}}$ is greater than $s_{s, \text{max}}$, a migration equilibrium exists. Next we show that $s_{s, \text{max}}$ is an increasing function of $q_j$ and $s_{p, \text{max}}$ is a decreasing function of $q_j$.

Finally, we show that when $q_j$ approaches 1, i.e. a country become very poor, $s_{s, \text{max}} > s_{p, \text{max}}$ and when $q_j$ approaches $q_j^*$, i.e. country is almost as rich as the rich country, $s_{s, \text{max}} < s_{p, \text{max}}$.

Then it is shown that there exists a particular value of $q_j$, at which $s_{s, \text{max}} = s_{p, \text{max}}$, which is the critical level of poverty.

Lemma 5.1 -

The maximum signal used in separation, $s_{s, \text{max}}$ is an increasing function of $\theta_j$. 

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Proof -
In order to prove the lemma, first we characterize \( s_{\text{max}} \), which is the maximum signal a high type agent is willing to issue in order to separate her from the low type. At this level of signal, the utility of migrating should at least be equal to the utility of not issuing any signal and not migrating. Using (5.10), this can be written as

\[
V_2 \left( s_{\text{max}}, H_1^* \right) = V_2 \left( 0, H_1 \right)
\]

The above condition implies that

\[
\frac{1}{(1-\alpha\beta)} \ln(h_{21,\text{max}} - f(s_{\text{max}})) + \frac{(1-\alpha)\beta}{(1-\beta)} \ln \left( \frac{1-\theta_1^* h_{21,\text{max}} + \theta_1^* h_{11,\text{max}}}{2-\theta_1} \right)
\]

\[
= \frac{1}{(1-\alpha\beta)} \ln h_{21,\text{max}} + \frac{(1-\alpha)\beta}{(1-\beta)} \ln \left( \frac{1-\theta_1 h_{21,\text{max}} + \theta_1 h_{11,\text{max}}}{2-\theta_1} \right)
\]

The lemma is then proven using the implicit function theorem. The proof is given in Appendix B.

Lemma 5.2 -
The maximum signal a low type agent is willing to issue, \( s_{\text{max}_p} \), is a decreasing function of \( \theta_1 \).

Proof -
The \( s_{\text{max}_p} \) is the maximum signal a low type agent is willing to issue in order to mimic the high type. This could be characterized by using condition (5.6). At the maximum signal,

\[
V_1 \left( 0, H_1 \right) = V_1 \left( s_{\text{max}_p}, H_1 \right)
\]

This implies

\[
= \frac{1}{(1-\alpha\beta)} \ln h_{11,\text{max}} + \frac{(1-\alpha)\beta}{(1-\beta)} \ln h_{11,\text{max}} =
\]

\[
\frac{1}{(1-\alpha\beta)} \ln (h_{11,\text{max}} - f(s_{\text{max}_p})) + \frac{(1-\alpha)\beta}{(1-\beta)} \ln \left( \theta_1 \left( h_{11,\text{max}} - f(s_{\text{max}_p}) \right) \right) + \left( (1-\theta_1) h_{21,\text{max}} - f(s_{\text{max}_p}) \right). \]
Lemma 5.3 -
When \( \theta_1 \to 1 \), then \( s_{p, max} < s_{s, max} \) and when \( \theta_1 \to \theta^*_1 \), then \( s_{p, max} > s_{s, max} \).

Proof -
Proof is given in Appendix B.

Proposition 5.1 -
If the proportion of low type agents in a poor country is above a critical value of \( \tilde{\theta} \), endogenously derived using other parameters of the model, a migration equilibrium can be supported. If the proportion is above the critical value, a no-migration equilibrium can be supported.

Proof -
Proof follows from Lemma 5.1 - Lemma 5.3.

VI. Coordination Failure, Multiple Equilibria and Threshold Poverty

In this part we use the strategic complementarity and coordination failure in order to establish the existence of multiple equilibria at a given level of poverty and the existence of threshold poverty level.

The “strategic complementarity” is the positive influence on any one agent’s utility by other agents’ actions as discussed in Cooper and John (1988). It is clear that any high type agent migrating will cause an impact on the utilities of other high type agents in the poor country. Hence there is a tendency for all high type agents to take similar actions. As already shown, in a no-migration equilibrium none of the high type agents issues a signal and migrates. This is an equilibrium because issuing no signal and not migrating is the best action when other high type do not migrate. However, we can further show that when this equilibrium occurs, it is likely that a migration equilibrium could also occur. This latter equilibrium occurs because if other high type agents issue signals and migrate, the best response by any single high type agent is also to issue a signal and migrate. This is stated in proposition 6.1.

When there is a migration equilibrium, a no-migration equilibrium could also be supported if a country is above the ‘threshold poverty level’ as stated in proposition 6.2. The threshold poverty level is defined as the boundary of poverty levels at which the migration equilibrium is the only equilibrium that could exist even with coordination failure.
A. Existence of Multiple Equilibria and Poverty Threshold

Assuming that one high type agent will issue a signal $s_i$ and other high type agents will issue $s_{-i}$, the value function of being in an environment with externality $H$ is written as $V(s_i, s_{-i}, H)$. For example, following this notation, the value function of a high type agent not issuing any signal and not migrating while others issue signals and migrating could be written as $V(0, s_{-i}, H)$. We use this notation when proving the following proposition.

**Proposition 6.1**

If the proportion of low type agents in a country is below the critical ratio, it could have at least two equilibria, migration and no-migration.

**Proof**

Existence of a no-migration equilibrium if the low type agents in a country is less than the critical ratio is already established in the proposition 5.1.

When all but one high type agent migrate, the situation is similar to a country with a very high proportion of low type agents. Hence the optimal action by any high type agent is to signal and migrate QED.

**Proposition 6.2**

When the proportion of low type agents in a country is higher than the critical ratio, two equilibria could exist if the country is not too poor.

**Proof**

We have already shown that when a country’s proportion of low type agents is higher than the critical ratio, a migration equilibrium exists. In order to prove that an agent’s action of not issuing a signal in response to other agents not issuing a signal and not migrating is optimal for a certain range of $\theta_j$, consider the utility of an agent issuing a signal and migrating when others do not issue signals and do not migrate. The agent will issue the minimum signal required for migration, which is $s_{p_{\text{max}}}$ and the utility is $V(s_{p_{\text{max}}}, 0, H_1^*)$, where

$$V(s_{p_{\text{max}}}, 0, H_1^*) = \ln k + \frac{1}{(1-\alpha\beta)} \ln \left( h_{21,\text{max}} - f \left( s_{p_{\text{max}}} \right) \right)$$

$$+ \frac{(1-\alpha)\beta}{(1-\beta)} \ln \left( \theta_1^* h_{11,\text{max}} + (1-\theta_1^*) h_{21,\text{max}} \right).$$

The externality is the rich country’s average level of human capital since migration of one agent does not change the average human capital level of the rich country significantly.

The utility of not issuing a signal when others do not issue a signal is $V(0, 0, H)$ as given in (5.9). For the existence of a no-migration equilibrium, it should be true that

$$V(s_{p_{\text{max}}}, 0, H_1^*) < V(0, 0, H_1) \quad (6.1)$$
In order to show this result, consider an implication of Lemma 5.3 which suggests that at the critical ratio of low type agents the following holds.

\[ V\left(s_{p_{\text{max}}}, s_{p_{\text{max}}}, H^*_1\right) = V\left(0, 0, H_1\right) \tag{6.2} \]

Assuming that when high type from the poor country migrates the externality of the rich country is greater, we can show that

\[ V\left(s_{p_{\text{max}}}, s_{p_{\text{max}}}, H^*_1\right) > V\left(s_{p_{\text{max}}}, 0, H^*_1\right) \tag{6.3} \]

Hence (6.1) holds as a strict inequality at the critical ratio of poverty.

According to Lemma 5.2, \( s_{p_{\text{max}}} \) is a decreasing and continuous function of \( \theta_1 \). Hence \( V(s_{p_{\text{max}}}, 0, H^*_1) \) is an increasing and continuous function of \( \theta_1 \). It can be shown that \( V(0, 0, H_j) \) is a decreasing and continuous function of \( \theta_j \). Hence, there exists a non-empty sub-set of \((\tilde{\theta}_1, 1]\) in which (6.1) holds as a weak inequality.

**B. Defining and Characterizing Threshold Poverty**

We define the threshold poverty as the lower bound of \( \theta_1 \) (\( \tilde{\theta}_1 \)) at which the inequality given in (6.1) does not hold. Hence, if a country has a proportion of low type agents higher than the threshold poverty level, strategic complementarity is not strong enough to support a no-migration equilibrium. The only equilibrium that can be supported is a migration equilibrium.

The threshold poverty can be characterized using (6.1) as an equality. Hence at the threshold poverty level,

\[ V\left(s_{p_{\text{max}}}, 0, H^*_1\right) = V\left(0, 0, H_1\right) \]

This implies

\[
\ln k + \frac{1}{(1-\alpha\beta)} \ln \left(h_{2,\text{max}} - f(s_{p_{\text{max}}})\right) + \frac{(1-\alpha)\beta}{(1-\beta)} \ln \left(h_{1,\text{max}}(1-\tilde{\theta}_1)\right) + \frac{(1-\theta_1)}{h_{2,\text{max}}(1-\tilde{\theta}_1)} = 0 \tag{6.4}
\]

The equation (6.4) suggests that the threshold poverty is an increasing function of the ratio of low type agents (\( \theta_1^* \)) in the rich country. At very low levels of \( \theta_1^* \), the threshold poverty may not exist since the rich country is too rich for an agent to be able to migrate. When \( \theta_1^* \) is too high, migration may not overcome the costs thus increasing the threshold poverty to a very high level. Figure 1 illustrates the boundary of threshold poverty.
C. Summary of Results

In this section we summarize the results obtained so far. The figure 2 shows the threshold poverty level and critical poverty level. The horizontal line in the figure depicts different poverty levels (ratio of the low type agents) of the poor country. Comparison of value functions in each region depicted in figure 2 is as follows.

1. In region 1, i.e. \([0, \theta)\)

Value of signaling and migrating when other high type agents migrate, \(V(s_{\text{max}}, s_{\text{max}}, H_1^*)\), is smaller than the value of not signaling and not migrating when others do not signal and do not migrate, \(V(0, 0, H_1)\), but it is larger than the value of not signaling and not migrating when others signal and migrate, \(V(0, s_{\text{max}}, H_1^*)\), and the value of signaling and migrating when others do not signal and migrate, \(V(0, s_{\text{max}}, H_1)\).

i.e. \(V(0, s_{\text{max}}, H_1^*) < V(0, 0, H_1) < V(s_{\text{max}}, s_{\text{max}}, H_1^*)\)

In this case most likely equilibrium is the no-migration equilibrium.

2. In region 2, i.e. \([\theta, \tilde{\theta})\)

Value of not signaling and not migrating when other high type agents do not signal and do not migrate, \(V(0, 0, H_1)\), is smaller than the value of signaling and migrating when others signal and migrate, \(V(s_{\text{max}}, s_{\text{max}}, H_1^*)\), but it is larger than the value of signaling and migrating when others do not signal and do not migrate, \(V(s_{\text{max}}, 0, H_1^*)\).

i.e. \(V(s_{\text{max}}, s_{\text{max}}, H_1^*) > V(0, 0, H_1) > V(s_{\text{max}}, 0, H_1^*)\)

In this case multiple equilibria could take place.

2. In region 3, i.e. \([\tilde{\theta}, 1)\)

Value of signaling and migrating is larger than value of not signaling and not migrating no matter what other agents do. i.e. \(V(0, 0, H_1^*) < V(s_{\text{max}}, s_{\text{max}}, H_1^*)\) and

\(V(0, 0, H_1^*) < V(s_{\text{max}}, 0, H_1^*)\). In this case only possibility is the migration equilibrium.
Figure 1 - Threshold Level of Poverty as a Function of the proportion of low type agents in the Rich country

![Figure 1](image)

Figure 2 - Comparison of Critical Poverty Level and the Threshold Poverty Level

Poverty Level (ratio of low type agents) →

0 no migration $\tilde{\theta}$ multiple eq. $\tilde{\theta}$ migration 1

Note: Critical Poverty Level - $\tilde{\theta}$ Threshold Poverty Level - $\tilde{\theta}$
VII. Welfare, Growth and Economic Policy

A. Welfare and Growth in a Closed Economy

Solutions given in (3.10) and (3.11) can be used to discuss the welfare and growth in a closed economy. A closed economy is considered as an environment where migration is not allowed. Hence agents do not signal, and the initial human capital level of an agent $i$ and the externality of the country are given by

$$H_1 = \sum_j \theta_j h_{j,\text{max}}$$

respectively. Using those solutions an agent $i$’s growth rates of human capital ($g_{hit}$), consumption ($g_{cit}$), and income ($g_{yit}$) at time $t$ can be derived.

$$g_{hit} = g_{cit} = g_{yit} = A(\alpha \beta) \alpha \left( \frac{\sum_j \theta_j h_{j,\text{max}}^{\alpha'}}{h_{1,\text{max}}^{\alpha' (1-\alpha)}} \right)^{1-\alpha}$$ (7.1)

The per capita income of the country is the weighted average of all agents’ income. The growth rate of per capita income is given in (7.2).

$$g_{yt} = \frac{\sum_j \theta_j y_{jt+1}}{\sum_j \theta_j y_{jt}} = \frac{\sum_j \theta_j u_{jt+1} h_{jt+1}}{\sum_j \theta_j u_{jt} h_{jt}} = A(\alpha \beta) \alpha \left[ \frac{\sum_j \theta_j h_{j,\text{max}}^{\alpha'} h_{jt+1}}{\sum_j \theta_j h_{j,\text{max}}^{\alpha'}} \right]^{\alpha}$$ (7.2)

Since $h_{20,\text{max}} > h_{10,\text{max}}$ and $\alpha < 1$, the following can be established.

i.) During the transition, the growth of low human capital agents is greater than that of high human capital agents in a given country. Furthermore, the low type will grow faster than the long run growth rate, whereas the high type will grow slower than the long run growth rate.

ii.) The growth rate per capita income of the country is slower than the long run growth during the transition period. This is because during the transition the high type grows slower than the long run growth of the country.

iii.) Human capital, consumption and income of any agent $i$ will eventually converge to the long run growth rate. i.e.,

$$\lim_{t \to \infty} g_{hit} = g_{cit} = g_{yit} \to A(\alpha \beta) \alpha.$$
iv). Human capital levels of all agents will converge to a common level, i.e.

\[
\lim_{t \to \infty} \frac{h_{i_t}}{h_{j_t}} \to 1; \forall i, j
\]

v). During the transition, the rich country will grow faster than the poor country.

Figure 3 describes the growth in the closed economy. The growth rate of low type agents’ income is greater than the long run steady growth during the transition as they are benefited by the higher average human capital in the country. The growth of the high type is lower due to the human capital externality.

**B. Welfare and Growth in an Open Economy with Full Information**

We have shown that in an open economy with full information all high type agents will migrate to the rich country. The impact of migration is shown in Figure 4. As seen in Figures 4a and 4b, the migration lowers the growth rate of low type agents in the poor country. Their income levels will fall leading to a loss of welfare (utility).

As discussed earlier, the per capita income of the country is the weighted average of agents’ income. As seen in Figure 4c, the growth of per capita income is slower than the long run growth during the period of transition. However after all high type agents migrate to the rich country, the growth rate of per capita income will converge to the long run rate leading to an increase in growth. The per capita income will drop sharply as shown in Figure 4d, but will grow faster afterwards. All agents in the rich country and its per capita income will grow faster as a result of migration. The welfare of migrants and both agent types in the rich country increases while the welfare of the low type agents in the poor country decreases.

**C. Welfare and Growth in an Open Economy with Private Information**

We have shown that if a country is above the threshold poverty level, multiple migration equilibria could exist. As seen in Figure 5, all agents in the rich country are benefited in a migration equilibrium. The low type agents in the poor country are hurt. Welfare of migrants is different depending on whether the country is below or above the critical poverty level. When the country is above the critical poverty level, (i. e. when it is not too poor) migrants’ welfare is lower in a migration equilibrium. Their welfare is greater if the country is below the critical poverty level.

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9/ A similar phenomenon occurs in the neo-classical growth model. Assuming the steady state of the model, consider loss of a part of physical capital. This will lower the income level of agents, but the economy will grow faster during the transition to the steady state.

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Figure 3 - Growth Rates of Different Agents’ Income and Per Capita Income in a Closed Economy

- Low Type
- All
- High Type

Figure 4 - Impact of Migration with full information on Growth Rates and Per Capita Income of the Poor Country

- a. Growth rate of low type agents’ income
- b. Level of low type agents’ income
- c. Growth rates of per capita income
- d. Level of per capita income
Figure 5 - Welfare Comparisons of Different Equilibria

a. Welfare in no-migration and migration equilibria when the proportion of low type is less than the critical poverty level

b. Welfare in no-migration and migration equilibria when the proportion of low type is higher than the critical poverty level
D. Policy Options

The policy for any country should be designed to enhance the benefits of its people. The policy options available for the rich country are straightforward. Their policy should be to impose the minimum required screening signal and allow the migration of high type agents. As explained in part 5, the rich country should not follow a policy of open liberalization, or should not randomly choose agents from poor countries, for it will reduce the average level of human capital in the rich country. There has to be a screening mechanism to allow self selection of high quality human capital to migrate. Policy options available to the poor country depends on how poor they are. If the poor country is above the critical poverty level, (i.e. if it is not too poor) policies on controlling migration will enhance the welfare of both agent types. However, if the country is below the critical poverty level or the threshold poverty level, controlling migration will hurt would-be migrants, but will help the low type. Hence the policy could be addressed in a political economy framework. The poor country could avoid herd behavior or mass migration arising from strategic complementarity by improving the economic and social infrastructure in the country.

VIII. Conclusion

Under the Mode 4 liberalization of services, natural persons can move freely between countries. As WTO explains the temporary nature of the movement of natural persons is defined negatively, to exclude permanent presence. The presence of natural persons in a host country has to be for a significantly longer period, since they have to establish service centers or join service centers domiciled in host countries.

WTO has noted that the Mode 4 liberalization has not taken place significantly, restricting the movement of natural persons. The model of migration with private information on agent types presented in this paper confirms this phenomenon of reluctance to freely liberalize the movement of natural persons. In this model, migration, or movement of natural persons for considerably longer periods, takes place from poor to rich countries, provided the host country adopts a liberal policy coupled with a costly screening system. The cost encourages self selection, where only those with considerably high human capital could migrate.

In this environment, there are no incentives to migrate if the source country is sufficiently rich. The incentive for migration increases as the degree of poverty in the source country increases. After a critical poverty level, multiple equilibria could emerge. But, if the poor country is below a “threshold poverty level” there can only be a migration equilibrium.

The different equilibria are the outcomes of costly signaling and strategic complementarity. A rich country can screen the high type by using an appropriately chosen level of observable human capital. If the poor country is considerably poor, the benefits of migration outweigh the costs leading to a migration equilibrium. However, for any high-type agent, the gap between costs and benefits depends on whether other high-type agents choose to issue a signal or not. This strategic complementarity of high type agents’ actions leads to two equilibria unless the poverty level of the country falls below the threshold poverty level. However, any high type agent living in a significantly poor country (falling below the threshold poverty level) will choose to migrate irrespective of the actions of other high type agents.
Migration reduces the income of low type agents and the per capita income of the poor country. However, after the migration takes place the per capita income of the poor country grows faster during the transition to the long run growth rate. This increase in per capita income growth is a result of the absence of high types in the country after migration whose growth in a closed economy is slower than the long run growth. After migration takes place only low types remain, and since they are homogenous, the country grows at the long run rate which is higher than the growth rate in a closed economy during the transition.

Migration always increases welfare in the rich country and reduces the welfare of low type agents in the poor country. The change in welfare of migrants depends on whether the poor country is above or below a “critical poverty level”. If the country is above the critical poverty level, i.e. not so poor, would-be migrants (i.e. high type agents in the poor country) will have a higher level of welfare in the no-migration equilibrium than in the migration equilibrium. Hence a no-migration equilibrium is preferred by both agent types. However, if the poor country is below the critical poverty level, the migration equilibrium increases the welfare of migrants. A poor country lying above the critical poverty level could draw appropriate economic policies to avoid the migration equilibrium, which will benefit all agents in the country. However, if a country is below the critical poverty level, there is no economic policy which will benefit all agent types. Hence policy could be a political outcome.

The policy for any country should be designed to enhance the benefits of its people. The policy options available for the rich country are straightforward. Their policy should be to impose the minimum required screening signal and allow the migration of high type agents. The rich country should not follow a policy of open liberalization, or should not randomly choose agents from poor countries as this will reduce the average level of human capital in the rich country.

Policy options available to the poor country depends on how poor they are. If the poor country is above the critical poverty level, i.e. if it is not too poor) policies on controlling migration will enhance the welfare of both agent types. However, if the country is below the critical poverty level or the threshold poverty level, controlling migration will hurt would-be migrants, but will help the low type. Hence the policy could be addressed in a political economy framework. The poor country could avoid herd behavior or mass migration arising from strategic complementarity by improving the economic and social infrastructure in the country.

The paper considered only a one-time migration. Continuing migration could be addressed when population growth is introduced to the model. This is left as a direction for future research.
References


APPENDIX A

DERIVING THE VALUE FUNCTION FOR THE MODEL

A. 1 Solution to the Set of First Order Conditions

Equation (3.4) gives
\[ \lambda_{it} = \frac{1}{c_{it}} = \frac{1}{u_{it}h_{it}} \quad (A.1) \]

Substituting \( t+1 \) for \( t \), (3.5) yields
\[ \lambda_{it+1}(1-u_{it+1}) = \mu_{it+1} \alpha A(1-u_{it+1})^{\alpha} h_{it+1}^{\alpha-1} H_{t+1}^{1-\alpha} \quad (A.2) \]

(A.2) in (3.8) yields,
\[ V_{it}'(h_{it+1}) = \lambda_{it+1} \quad (A.3) \]

(A.3) and (3.6) could be used to produce
\[ \mu_{it} = \beta \lambda_{it+1} \quad (A.4) \]

(A.1) yields
\[ \frac{\lambda_{it+1}}{\lambda_{it}} = \frac{u_{it}h_{it}}{u_{it+1}h_{it+1}} \quad (A.5) \]

Using (A.4), (A.5) can be written as
\[ \frac{\mu_{it}}{\beta \lambda_{it}} = \frac{u_{it}h_{it}}{u_{it+1}h_{it+1}} \quad (A.6) \]

Using (3.5) again and substituting the budget constraint for \( h_{it+1} \), (A.6) is rewritten as
\[ u_{it+1}(1-u_{it}) - \alpha \beta u_t = 0 \quad (A.7) \]

Fixed points of the difference equation in (A.7) are \( 0 \) and \( (1-\alpha\beta) \). We also have \( \frac{\partial u_{it+1}}{\partial u_t} = 1 / \alpha \beta \), \( >1 \). Hence using the transversality condition we can deduce that the system does not show any transitional dynamics. The stationary labor choice is \( (1-\alpha\beta) \).
A.2. Human Capital Accumulation Process

Using the result in A1, the following process is derived.

\[ h_{t2} = A(\alpha \beta)^{\alpha} h_{t1}^{\alpha} H_{1}^{1-\alpha} \]
\[ h_{t3} = A(\alpha \beta)^{\alpha} h_{t2}^{\alpha} H_{2}^{1-\alpha} \]
\[ = A(\alpha \beta)^{\alpha} \left( \sum \theta_j A(\alpha \beta)^{\alpha} h_{t1}^{\alpha} H_{1}^{1-\alpha} \right)^{1-\alpha} \]
\[ = A^2(\alpha \beta)^{2\alpha} h_{t1}^{\alpha 2} H_{1}^{1-\alpha} \left( \sum \theta_j h_{j1}^{\alpha} \right)^{1-\alpha} \]
\[ h_{t4} = A(\alpha \beta)^{\alpha} h_{t3}^{\alpha} H_{3}^{1-\alpha} \]
\[ = A(\alpha \beta)^{\alpha} \left( \sum \theta_j h_{j1}^{\alpha} \right)^{1-\alpha} \left( \sum \theta_j A(\alpha \beta)^{\alpha} h_{t1}^{\alpha} H_{1}^{1-\alpha} \left( \sum \theta_j h_{j1}^{\alpha} \right)^{1-\alpha} \right)^{1-\alpha} \]
\[ = A^3(\alpha \beta)^{3\alpha} h_{t1}^{\alpha 3} H_{1}^{1-\alpha} \left( \sum \theta_j h_{j1}^{\alpha} \right)^{1-\alpha} \left( \sum \theta_j h_{j1}^{\alpha} \right)^{1-\alpha} \]
\[ = A^3(\alpha \beta)^{3\alpha} h_{t1}^{\alpha 3} H_{1}^{1-\alpha} \left( \sum \theta_j h_{j1}^{\alpha} \right)^{1-\alpha} \left( \prod_{s=1}^{2} \sum \theta_j h_{j1}^{\alpha} \right)^{1-\alpha} \]

Hence

\[ h_{it} = \left( A^{1/\alpha} \alpha \beta \right)^{\alpha i} h_{t1}^{\alpha i} \prod_{s=0}^{i-1} \left( \sum \theta_j h_{j1}^{\alpha i} \right)^{1-\alpha} \quad (A.8) \]
A.3. Consumption Path

\[ c_{it} = u_i h_{it} = (1 - \alpha \beta)^t (A(\alpha \beta)^t \alpha \beta \beta_1 \prod_{s=1}^{t-1} \sum_j \theta_j h_{j1}^{\alpha \beta})^{1-\alpha} \]

\[ = (1 - \alpha \beta)^t A' (\alpha \beta)^t h_{11}^{\alpha \beta} \prod_{s=0}^{t-1} \sum_j \theta_j h_{j1}^{\alpha \beta}]^{1-\alpha} \] (A.9)

A.4. Value Function

\[ V_i = \sum_{t=0}^{\infty} \beta^t \ln c_{it} \]

\[ = \sum_{t=0}^{\infty} \beta^t \ln (1 - \alpha \beta)^t (A(\alpha \beta)^t \alpha \beta \beta_1 \prod_{s=0}^{t-1} \sum_j \theta_j h_{j1}^{\alpha \beta})^{1-\alpha} \]

\[ = \sum_{t=0}^{\infty} \beta^t \ln (1 - \alpha \beta) + \sum_{t=0}^{\infty} \beta^t \ln (A(\alpha \beta)^t \alpha \beta \beta_1 \prod_{s=0}^{t-1} \sum_j \theta_j h_{j1}^{\alpha \beta})^{1-\alpha} \]

\[ = \sum_{t=0}^{\infty} \beta^t \ln (1 - \alpha \beta) + \sum_{t=0}^{\infty} \beta^t \ln A(\alpha \beta)^t \alpha \beta \beta_1 + \sum_{t=0}^{\infty} \beta^t \ln \prod_{s=0}^{t-1} \sum_j \theta_j h_{j1}^{\alpha \beta}]^{1-\alpha} \] (A.10)

In order to further simplify (A.10), following results are used.

\[ \sum \beta^t = \frac{1}{1 - \beta} \] (A.11)
\[\sum \beta^i t = \beta + 2\beta^2 + 3\beta^3 + \ldots = \beta + \beta^2 + \beta^3 + \beta^3 + \beta^4 + \ldots = \beta \left( \frac{1}{1 - \beta} \right) + \beta^2 \left( \frac{1}{1 - \beta} \right) + \ldots = \frac{\beta}{(1 - \beta)^2} \]  

(A.12)

(A.11) and (A.12) in (A.10),

\[V_i = \frac{\ln(1 - \alpha\beta)}{(1 - \beta)} + \frac{\beta}{(1 - \beta)^2} \ln A(\alpha\beta)^\alpha + \frac{1}{(1 - \alpha\beta)} \ln h_{i1} + (1 - \alpha) + \frac{(1 - \alpha)\beta}{(1 - \beta)} \ln \left( \sum_j \theta_j h_{j1} \right) + \frac{(1 - \alpha)}{(1 - \beta)} \sum_{t=2}^{\infty} \beta^t \ln \left( \sum_j \theta_j h_{j1}^t \right).\]

Consider \(\sum_{j=1}^{12} \theta_j h_{j1}^t\) appeared in (3.8). It should be noted that for large values of t, \(\sum_{j=1}^{12} \theta_j h_{j1}^t\) reduces to 1 and the log of this value is zero. All other terms of \(h_{j1}^\alpha\) are considered significantly smaller than \(h_{j1}\). Hence value function can be written as

\[V_i = \frac{\ln(1 - \alpha\beta)}{(1 - \beta)} + \frac{\beta}{(1 - \beta)^2} \ln A(\alpha\beta)^\alpha + \frac{1}{(1 - \alpha\beta)} \ln h_{i1} + (1 - \alpha) + \frac{(1 - \alpha)\beta}{(1 - \beta)} \ln \left( \sum_j \theta_j h_{j1} \right).\]  

(A.13)
APPENDIX B

PROOFS OF LEMMAS 5.1 - 5.3

B. 1 Proof of Lemma 5.1

Equation (5.11) could be written as

\[ F_1 = \frac{1}{1-\alpha\beta} \ln \left( \frac{h_{21,\text{max}} - f(s_{s,\text{max}})}{h_{21,\text{max}}} \right) \]

\[ + \frac{(1-\alpha)\beta}{1-\beta} \ln \left( \frac{1-\theta h_{21,\text{max}} + \frac{\theta}{2-\theta} h_{11,\text{max}} + \frac{1-\theta}{2-\theta} \left( h_{21,\text{max}} - f(s_{s,\text{max}}) \right)}{(1-\theta)h_{21,\text{max}} + \theta h_{11,\text{max}}} \right) = 0 \]  \hspace{1cm} (B.1)

Implicit function theorem states that

\[ \frac{\partial s_{s,\text{max}}}{\partial \theta_1} = - \frac{\frac{\partial F_1}{\partial \theta_1}}{\frac{\partial F_1}{\partial s_{s,\text{max}}}} \]  \hspace{1cm} (B.2)

Using the result \( f' > 0 \) discussed in Part1, \( \frac{\partial F_1}{\partial s_{s,\text{max}}} \) is <0 and \( \frac{\partial F_1}{\partial \theta_1} \) is >0. Hence we can show that \( \frac{\partial s_{s,\text{max}}}{\partial \theta_1} > 0 \).
B.2. Proof of Lemma 5.2.

Equation (5.12) can be re-written as

\[
F_2 = \frac{1}{1 - \alpha \beta} \ln \left( \frac{h_{11,\text{max}} - f(s_{p,\text{max}})}{h_{11,\text{max}}} \right) \\
+ \frac{(1 - \alpha) \beta}{1 - \beta} \ln \left( \frac{\theta \left( h_{11,\text{max}} - f(s_{p,\text{max}}) \right) + (1 - \theta) \left( h_{21,\text{max}} - f(s_{p,\text{max}}) \right)}{h_{11,\text{max}}} \right)
\]

Using result \( f' > 0 \), it is easy to show that \( \frac{\partial F_1}{\partial s_{p,\text{max}}} < 0 \). It can also be shown that \( \frac{\partial F_1}{\partial \theta_1} < 0 \). Hence the implicit function theorem derives the result.

B.3 Proof of Lemma 5.3

The proposition is proved by examining the functions \( F_1 \) and \( F_2 \) defined above.

Using \( F_2 \) it is easy to show that when \( \theta_1 \to 1 \), then \( s_{p,\text{max}} \to 0 \). Using \( F_1 \) it could be shown that when \( \theta_1 \to 1 \), \( s_{s,\text{max}} \) should remain non zero for \( F_1 \) to hold. Hence when \( \theta_1 \to 1 \), then \( s_{p,\text{max}} < s_{s,\text{max}} \).

Consider \( \theta_1 \to \theta^*_1 \).

Then \( F_1 \) and \( F_2 \) takes following forms.
\[ F_1\left( \theta^*_1, s_{s, \max} \right) = \frac{1}{1 - \alpha \beta} \ln \left( \frac{h_{21, \max} - f(s_{s, \max})}{h_{21, \max}} \right) \]

\[ + \frac{(1 - \alpha) \beta}{(1 - \beta)} \ln \left( \frac{1 - \theta^*_1}{2 - \theta^*_1} \frac{h_{21, \max}}{h_{10, \max}} + \frac{\theta^*_1}{2 - \theta^*_1} \frac{h_{10, \max}}{h_{21, \max}} + \frac{1 - \theta^*_1}{2 - \theta^*_1} \frac{h_{21, \max} - f(s_{s, \max})}{h_{21, \max} - f(s_{s, \max})} \right) = 0 \quad (B.4) \]

and

\[ F_2\left( \theta^*_1, s_{p, \max} \right) = \frac{1}{1 - \alpha \beta} \ln \left( \frac{h_{1, \max} - f(s_{p, \max})}{h_{10, \max}} \right) \]

\[ + \frac{(1 - \alpha) \beta}{(1 - \beta)} \ln \left( \frac{\theta^*_1}{h_{1, \max}} \frac{h_{1, \max} - f(s_{p, \max})}{h_{10, \max}} + \frac{1 - \theta^*_1}{h_{1, \max}} \frac{h_{1, \max} - f(s_{p, \max})}{h_{10, \max}} \right) = 0 \quad (B.5) \]

We wish to show that the root of \( F_1\left( \theta^*_1, s_{s, \max} \right) = 0 \), is smaller than the root of \( F_2\left( \theta^*_1, s_{p, \max} \right) = 0 \). In order to show this, we establish that on the F - s plane,

i. both \( F_1\left( \theta^*_1, s_{s, \max} \right) \) and \( F_2\left( \theta^*_1, s_{p, \max} \right) \) are concave downward, and

ii. \( F_2\left( \theta^*_1, s_{p, \max} \right) \) lies above \( F_1\left( \theta^*_1, s_{s, \max} \right) \) until \( F_1\left( \theta^*_1, s_{s, \max} \right) \) approaches the value zero.
Both functions can be proved concave downward by examining the first and second derivatives. The strict convexity of cost functions of signaling ($f_1$ and $f_2$) ensures the property (i) above.

In order to show the property (ii) above, consider the behavior of two functions at $s=0$.

\[
F_1(\theta_1^*,0) = \frac{(1-\alpha)\beta}{(1-\beta)} \ln \left[ \frac{(1-\theta_1^*)h_{21,max} + \theta_1^* h_{11,max} + (1-\theta_1^*)h_{21,max}}{(1-\theta_1^*)h_{21,max} + \theta_1^* h_{11,max}} \right] \left(2-\theta_1^*\right) \tag{B.6}
\]

\[
F_2(\theta_1^*,0) = \frac{(1-\alpha)\beta}{(1-\beta)} \ln \left[ \frac{(1-\theta_1^*)h_{21,max} + \theta_1^* h_{11,max}}{h_{11,max}} \right] \tag{B.7}
\]

For $F_2(\theta_1^*,0) > F_1(\theta_1^*,0)$, it should be the case that

\[
\left[ \frac{(1-\theta_1^*)h_{21,max} + \theta_1^* h_{11,max}}{h_{11,max}} \right] > \left[ \frac{(1-\theta_1^*)h_{21,max} + \theta_1^* h_{11,max} + (1-\theta_1^*)h_{21,max}}{h_{11,max}} \right] \left(2-\theta_1^*\right) \tag{B.8}
\]

Define $z=h_{20,max}/h_{10,max}$. Then, (B.8) becomes,

\[
\theta_1^* + (1-\theta_1^*)z > \left[ \frac{2(1-\theta_1^*)z + \theta_1^*}{\theta_1^* + (1-\theta_1^*)z})\right] \left(2-\theta_1^*\right) \]

re-arranging,

\[
z^2 - z\left[ \frac{2(1-\theta_1^*)}{2-\theta_1^*} \right] > \frac{\theta_1^*}{(2-\theta_1^*)} \]

\[
\left[ z - \frac{1-\theta_1^*}{2-\theta_1^*} \right]^2 > \frac{\theta_1^*}{(2-\theta_1^*)} + \left[ \frac{1-\theta_1^*}{2-\theta_1^*} \right]^2 = \frac{1}{(2-\theta_1^*)^2}
\]
\[ z > \frac{1 - \theta_1^*}{2 - \theta_1^*} \pm \frac{1}{2 - \theta_1^*} \]

i.e. \[ z > \frac{-\theta_1^*}{2 - \theta_1^*} \text{ or } 1 \]  \hspace{1cm} (B.9)

Since \( z > 1 \), the inequality holds.

In order to prove the Lemma, we should show that \( F_2 \) lies above \( F_1 \) everywhere on \( s \), until \( F_1 \) approaches zero or any negative value. This can be shown using the value of \( s \), which is the maximum signal that will still keep the human capital level of a high type agent greater than the average human capital level of the rich country. The value of \( s, s_{\text{max}} \), can be derived using the following constraint.

\[ h_{2,1,\text{max}} - f(s) > \theta_1^* h_{1,1,\text{max}} + (1 - \theta_1^*) h_{2,1,\text{max}} \]

\[ \Rightarrow f(s_{\text{max}}) = h_{2,1,\text{max}} - \theta_1^* h_{1,1,\text{max}} - (1 - \theta_1^*) h_{2,1,\text{max}} \]  \hspace{1cm} (B.10)

We will show that at this level of \( s, F_2 > F_1 \) and \( F_1 < 0 \).

\[ F_1(\theta_1^*, s_{\text{max}}) = \frac{1}{(1 - \alpha \beta)} \ln \left( 1 - \theta_1^* \left( \frac{h_{2,1,\text{max}} - h_{1,1,\text{max}}}{h_{2,1,\text{max}}} \right) \right) \text{ which is } < 0. \]  \hspace{1cm} (B.11)

\[ F_2(\theta_1^*, s_{\text{max}}) = \frac{1}{(1 - \alpha \beta)} \left[ \ln \left( 1 - \theta_1^* \left( \frac{h_{2,1,\text{max}} - h_{1,1,\text{max}}}{h_{1,1,\text{max}}} \right) \right) + \frac{\alpha \beta}{1 - \beta} \ln \left( \frac{h_{2,1,\text{max}}}{h_{1,1,\text{max}}} - 2 \theta_1^* \left( \frac{h_{2,1,\text{max}} - h_{1,1,\text{max}}}{h_{1,1,\text{max}}} \right) \right) \right] \]  \hspace{1cm} (B.12)

For \( \theta_1^* < 0.5 \), \( F_2(\theta_1^*, s_{\text{max}}) > 0 > F_1(\theta_1^*, s_{\text{max}}) \).

The proof then follows.